# A Method to Estimate the Probability that any Individual Lightning Stroke Contacted the Surface within any Radius of any Point 

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## 1 Introduction

The estimation of the probability of an individual nearby lightning stroke contacting the surface within a specified distance of a specified spaceport processing facility is important to allow engineers to decide if inspection of electronics for damage from induced currents from that stroke is warranted. If induced current damage has occurred, inspections of the electronics are critical to identify required fixes and avoid degraded performance or failure of the satellite or space launch vehicle. However, inspections are costly both financially and in terms of delayed processing for space launch activities. As such, it is important these inspections be avoided if not needed. At Kennedy Space Center (KSC) and Cape Canaveral Air Force Station (CCAFS), one of the main purposes of the Four Dimensional Lightning Surveillance System (4DLSS) [8],[9] is detection of nearby strokes and determination of their peak current to support those inspection decisions [5],[6],[10]. The high frequency of occurrence of lightning in East Central Florida combined with the large amount of complex sensitive electronics in satellite payloads, space launch vehicles, and associated facilities make those decisions critically important to space launch processing. While 4DLSS provides the
data for 95th or 99th percentile location error ellipses for the best location for each stroke, depending on customer, it has not been able to provide the probability for the stroke being within a customer specified distance of a point of interest. This paper presents a new method to convert the 4DLSS error of 50th percentile location error ellipse for best location of any stroke into the probability that the stroke was within any radius of any facility at CCAFS/KSC. This new facility-centric technique is a significant improvement over the stroke-centric location error ellipses the 45th Weather Squadron (45WS) was providing. This technique is adapted from a method of calculating the probability of debris collision with spacecraft.[1],[2],[3],[7] A table of abbreviations used in this paper is available in Section 7, Table 2.

## 2 Background

In spacecraft collision probability and the other applications, at the instant of "nominal" closest approach, the position uncertainty of the collision object relative to the asset is described by a bivariate Gaussian probability density function (pdf).[1],[2],[3]

$$
\begin{aligned}
& f_{2}(x, z)=\frac{1}{2 \pi \sigma_{x} \sigma_{z} \sqrt{1-\rho_{x z}^{2}}} * \\
& e^{-\left[\left(\frac{x}{\sigma_{x}}\right)^{2}-2 \rho_{x x}\left(\frac{x}{\sigma_{x}}\right)\left(\frac{z}{\sigma_{z}}\right)+\left(\frac{z}{\sigma_{z}}\right)^{2}\right] / 2\left(1-\rho_{x z}^{2}\right)}
\end{aligned}
$$

where $\sigma_{x}$ and $\sigma_{z}=$ the standard deviations of $x$ and $z, \rho_{x z}=$ correlation coefficient of $x$ and $z, x$ and $z$ are the designations for the rectangular coordinates in the collision plane.

The probability of collision is given by the two-dimensional integral, where $A$ is the collision cross-sectional area which is a circle with radius, $\mathrm{r}_{\mathrm{A}}$.[3]

$$
P=\iint_{A} f_{2}(x, z) d x d z
$$

There is no known analytical solution to the above integral when the two standard
deviations $\sigma_{x}$ and $\sigma_{z}$ are not equal. The solution is based either on transforming the two dimensional Gaussian probability distribution function (pdf) to a onedimensional Rician pdf and using the concept of equivalent areas or by performing a numerical integration of the two dimensional Gaussian pdf.[1],[2],[3]

The geometry used for spaceflight collision probability can also be used for estimation of the probability of an individual nearby lightning stroke contacting the surface within a specified distance of a specified point of interest as shown in Figure 1 below. Both solution methods, numerical integration as well as the analytical method of equivalent areas using the Rician pdf, will be analyzed in the next section.


Figure 1. Schematic diagram of the angles used in probability calculation for a sample lightning location error ellipse. $\alpha$ is the heading of the semi-major axis of the lightning location uncertainty ellipse from true north. $\theta$ is the angle between the semi-major axis of the lightning location uncertainty ellipse and line connecting the center of the lightning uncertainty ellipse and the center of the area of interest.

## 3 Evaluation

The probability that any lightning strike is within any radius of any point of interest would be extremely difficult to estimate intuitively. As a result, given the high impact resultant decisions, the tool must be extensively tested. Three major types of tests were conducted and are discussed in the following sections: 1) known mathematical solutions (Test Set 1), 2) expected behavior as single parameters are varied (Test Set 2), and 3) examination of real-world events (Test Set 3 and Test Set 4). The new technique passed all of the tests.

### 3.1 Test Set 1

The first set of testing compared the probability calculated by the program to the corresponding circular probability from the CRC Handbook of Tables for Probability and Statistics.[4] Table 1 shows, for various inputs, the calculated probability and the CRC Handbook probability. The values matched to within a tenth of a percent. These differences in the final digit may be due to round-off error.

| Semi- <br> major <br> Axis <br> (nmi) | Semi- <br> minor <br> Axis <br> (nmi) | Heading of <br> semi-major <br> axis from <br> true North | POI lat | POI lon | Strike <br> Lat | Strike <br> Lon | Radius <br> around <br> POI <br> (nmi) | Calculated <br> probability | CRC <br> Hand- <br> book <br> prob- <br> ability $[4]$ |
| :---: | :---: | :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 3 | 15 | 28.60827 | -80.6041 | 28.6995 | -80.6041 | 3 | 0.095 | 0.095 |
| 3 | 3 | 15 | 28.60827 | -80.6041 | 28.631 | -80.6041 | 3 | 0.453 | 0.452 |
| 3 | 3 | 15 | 28.60827 | -80.6041 | 28.608 | -80.6041 | 3 | 0.500 | 0.499 |
| 1 | 1 | 15 | 28.60827 | -80.6041 | 28.608 | -80.6041 | 1 | 0.500 | 0.499 |
| 1 | 1 | 15 | 28.60827 | -80.6041 | 28.631 | -80.6041 | 1 | 0.200 | 0.200 |
| 1 | 1 | 15 | 28.60827 | -80.6041 | 28.6995 | -80.6041 | 1 | 0.000 | 0.000 |
| 1 | 1 | 15 | 28.60827 | -80.6041 | 28.608 | -80.6041 | 2 | 0.937 | 0.938 |

Table 1. Calculated probability vs. CRC Handbook probability for various inputs. The abbreviations are defined as follows.

| Abbreviation | Definition |
| :--- | :--- |
| conf | confidence |
| CE | confidence ellipse |
| lat | latitude |
| lon | longitude |
| nmi | nautical miles |
| POI | point of interest |

### 3.2 Test Set 2

The second type of testing involved plotting the calculated probabilities as particular inputs were varied while holding the other inputs constant and comparing them to an independently coded program written by Dr. F. Kenneth Chan of the Aerospace Corporation and the author of "Spacecraft Collision Probability".[3] Also tested was the difference between using a numerical integration technique for calculating the probability versus an analytical technique, shown as "Rician" in the results below. The analytical or Rician technique involves transforming the two dimensional Gaussian pdf to a onedimensional Rician pdf and using the concept of equivalent areas to calculate the probability.[1],[2],[3] The results are shown in Figures 2 through 5 and 8 below. The data used to generate these figures are in Table 2. Note that results using the 45WS and Chan's program match almost exactly regardless of integration method used. Probability calculations are much faster using the analytical technique as opposed to the numerical integration technique. Therefore, it was of interest to understand the conditions in which the analytical technique performed well compared to the numerical integration technique. The numerical integration technique and the analytical integration technique tend to diverge as the ratio of the semi-major axis to semi-minor axis increases and as the orientation angle of the ellipse approaches 0 or 180 degrees.

Figure 2 shows the change in probability as a result of changing the radius around the point of interest while holding all other parameters constant. Chan's probability calculated using both the numerical integration technique as well as the analytical (Rician) technique is compared to the probability calculated
using the 45WS program. The worst case probability difference between methods is $0.25 \%$ at a radius of 2 nautical miles around the point of interest. Chan's probability using both techniques matches the 45WS probability exactly at all radii.

Figure 3 shows the change in probability as a result of changing the latitude of the strike from the point of interest while holding all other parameters constant. Chan's probability calculated using both the numerical integration technique as well as the analytical (Rician) technique is compared to the probability calculated using the 45WS program. The probability follows a Gaussian curve and reaches a maximum when the uncertainty ellipse is at its closest point of approach to the point of interest, as expected. The worst case probability difference between methods is 0.06 where the lightning stroke is at latitude of $28.6162^{\circ} \mathrm{N}$, which is about 0.5 nautical miles away from the point of interest. Chan's probability using both techniques matches the 45WS probability exactly at all latitudes.

Figure 4 shows the change in probability as a result of changing the longitude of the strike from the point of interest while holding all other parameters constant. Chan's probability calculated using both the numerical integration technique as well as the analytical (Rician) technique is compared to the probability calculated using the 45WS program. The probabilities follow a Gaussian curve and reach a maximum when the uncertainty ellipse is at its closest point of approach to the point of interest, as expected. The worst case probability difference between methods is 0.08 where the lightning stroke is at a longitude of $80.5961^{\circ} \mathrm{W}$, which is about 0.4 nautical miles away from the point of interest. Chan's probability using both
techniques matches the 45WS probability exactly at all longitudes.

Figure 5 shows the change in probability as a result of changing the heading from true north of the semi-major axis of the lightning uncertainty ellipse while holding all other parameters constant. Chan's probability calculated using both the numerical integration technique as well as the analytical (Rician) technique is compared to the probability calculated using the 45WS program. The center of the stroke uncertainty ellipse is located about 0.5 nautical miles away from the point of interest. The probabilities show a roughly sinusoidal pattern as more then less then more again of the ellipse rotates into, out of, then into the area around the point of interest. However, the difference in probability between the two integration techniques is enhanced as the ellipse is rotated. The worst case probability difference between methods is 0.28 where the lightning stroke heading is at an angle of $0^{\circ}$ or $180^{\circ}$ from true north.

Figures 6 and 7 show a Google Maps visualization of the $99 \%$ confidence lightning uncertainty ellipse as it is rotated from $180^{\circ}$ to $90^{\circ}$ from true north. The lightning uncertainty ellipse at a heading of $90^{\circ}$ from true north is the rotation angle at which there is no difference in the probability calculated by the numerical integration technique and the analytical (Rician) technique. Chan's probability
using both techniques matches the 45WS probability exactly at all angles.

Figure 8 shows the change in probability as a result of varying the aspect ratio (length of semi-major axis/length of semi-minor axis) of the lightning uncertainty ellipse from 1.5 to 11 with the strike point close to the point of interest while holding all other parameters constant. Chan's probability calculated using both the numerical integration technique as well as the analytical (Rician) technique is compared to the probability calculated using the 45WS program. The probability becomes less as the aspect ratio of the uncertainty ellipse is larger. However, the difference in probability between the two integration techniques is enhanced as the aspect ratio is increased. The worst case probability difference between methods is 0.07 where the aspect ratio is 8 . Chan's probability using both techniques matches the 45WS probability exactly at all aspect ratios.

In light of the results of the differences between calculations (numerical integration vs. analytical [Rician] method), the 45 WS has decided to use the numerical integration technique to calculate probabilities. Although the program run time is longer using the numerical integration technique, the accuracy improvements justify the longer calculation time.

| Figure | Semimajor axis of 50\% CE (nmi) | Semiminor axis of 50\% CE (nmi) | Confidence | Heading <br> (from <br> true <br> North) <br> of semi- <br> major <br> axis | $\begin{array}{lc} \hline \mathrm{POO} & \text { lat } \\ \left({ }^{\circ} \mathrm{N}\right) \end{array}$ | POI Ion ( ${ }^{\circ} \mathrm{W}$ ) | Strike lat ( ${ }^{\circ} \mathrm{N}$ ) | Strike Ion ( ${ }^{\circ} \mathrm{W}$ ) | Radius around POI (nmi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 3.1 | 1.2 | 0.50 | 75 | 28.60827 | 80.6041 | 28.59 | 80.59 | Varied |
| 3 | 0.3 | 0.2 | 0.50 | 44.3 | 28.60827 | 80.6041 | Varied | 80.6041 | 0.45 |
| 4 | 0.3 | 0.2 | 0.50 | 44.3 | 28.60827 | 80.6041 | 28.6082 | Varied | 0.45 |
| 5 | 0.3 | 0.2 | 0.50 | Varied | 28.60827 | 80.6041 | 28.6162 | 80.6041 | 0.45 |
| 6 | 0.3 | 0.2 | 0.50 | 180 | 28.60827 | 80.6041 | 28.6162 | 80.6041 | 0.45 |
| 7 | 0.3 | 0.2 | 0.50 | 90 | 28.60827 | 80.6041 | 28.6162 | 80.6041 | 0.45 |
| 8 | Varied | 0.1 | 0.50 | 90 | 28.60827 | 80.6041 | 28.6062 | 80.6041 | 0.45 |

Table 2. Input values used for scenarios shown in Figures 2 through 8. The abbreviations are the same as defined in Table 1.


Figure 2. Change in probability as a result of changing the POI radius while holding all other parameters constant.


Figure 3. Change in probability as a result of changing the strike lat from the POI while holding all other parameters constant.


Figure 4. Change in probability as a result of changing the strike lon of the strike from the POI while holding all other parameters constant.


Figure 5. Change in probability as a result of changing the semi-major axis heading of the lightning uncertainty ellipse while holding all other parameters constant.


Figure 6. Google Maps visualization of a lightning uncertainty ellipse overlaid on the radius around the POl with a semimajor axis heading of $180^{\circ}$ as graphed in Figure 5.


Figure 7. Google Maps visualization of a lightning uncertainty ellipse overlaid on the radius around the POI with a semimajor axis heading of $90^{\circ}$ as graphed in Figure 5.


Figure 8. Change in probability as a result of varying the aspect ratio (length of semi-major axis/length of semi-minor axis) of the lightning uncertainty ellipse from 1.5 to 11 with the strike point close to the POI while holding all other parameters constant.

### 3.3 Test Set 3

The third type of testing analyzed six real-world lightning strikes near Space Launch Complex 39A on 3 August 2009. Figure 9 shows the spreadsheet used to generate the lightning report for those six strikes. Additional data on these strikes are in Table 3. These strikes were selected because the closest point on the lightning position uncertainty ellipse was within 0.45 nautical miles of Launch Complex 39A. Figures 10 through 15 are Google Maps depictions of these six strokes. The probabilities for a small area around a facility, even for a nearby stroke, may appear to be surprisingly low. For example, one strike just 0.65 nautical miles away (Figure 14) had only a $0.7 \%$ probability of being within the 0.45 nautical mile radius of Launch Complex 39A. All calculated probabilities are consistent with these real-world events.


Figure 9. Sample of lightning strikes where the closest point on the lightning position uncertainty ellipse was within 0.45 nmi of Launch Complex 39A on 3 August 2009.

| Figure | Semi- <br> major <br> axis <br> of <br> 50\% <br> CE <br> (nmi) | Semiminor axis of 50\% CE (nmi) | Confidence | Heading <br> (from <br> true <br> North) <br> of semi- <br> major <br> axis | POI lat <br> ( ${ }^{\circ} \mathrm{N}$ ) | POI Ion ( ${ }^{\circ} \mathrm{W}$ ) | Strike lat <br> ( ${ }^{\circ} \mathrm{N}$ ) | Strike Ion ( ${ }^{\circ} \mathrm{W}$ ) | Radius around POI (nmi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 0.15 | 0.05 | 0.99 | 301.5 | 28.60827 | 80.6041 | 28.6107 | 80.6124 | 0.45 |
| 11 | 0.2 | 0.1 | 0.99 | 300.7 | 28.60827 | 80.6041 | 28.6114 | 80.6113 | 0.45 |
| 12 | 0.15 | 0.05 | 0.99 | 301.3 | 28.60827 | 80.6041 | 28.6122 | 80.6147 | 0.45 |
| 13 | 0.15 | 0.1 | 0.99 | 293 | 28.60827 | 80.6041 | 28.6178 | 80.6069 | 0.45 |
| 14 | 0.6 | 0.2 | 0.99 | 88.8 | 28.60827 | 80.6041 | 28.6041 | 80.6317 | 0.45 |
| 15 | 0.3 | 0.2 | 0.99 | 293 | 28.60827 | 80.6041 | 28.6178 | 80.6069 | 0.45 |

Table 2. Input values used for scenarios shown in Figures 10 through 15. The abbreviations are the same as defined in Table 1.


Figure 10. Google Maps visualization of the $99 \%$ conf uncertainty ellipse for the closest lightning strikes to Complex 39A on 03 August 2009. There is a $45.9 \%$ probability that the lightning strike occurred within the 0.45 nmi radius.


Figure 11. Google Maps visualization of the $99 \%$ conf uncertainty ellipse for one of the closest lightning strikes to Complex 39A on 03 August 2009. The center of the ellipse was within the 0.45 nmi radius. There is a $54.4 \%$ probability that the lightning occurred within that radius.


Figure 12. Google Maps visualization of the $99 \%$ conf uncertainty ellipse for a lightning strike near Complex 39A on 03 August 2009. Figure 12 shows a probability of $10.4 \%$ of the lightning strike occurring within the 0.45 nmi radius.


Figure 13. Google Maps visualization of the $99 \%$ conf uncertainty ellipse for a lightning strike near Complex 39A on 03 August 2009. Figure 13 shows a probability of $6.4 \%$ of the lightning strike occurring within the 0.45 nmi radius.


Figure 14. Google Maps visualization of the 99\% confidence uncertainty ellipse for nearby lightning strike to Complex 39A on 03 August 2009. Figure 14 shows a probability of $0.7 \%$ of the lightning strike occurring within the 0.45 nmi radius.


Figure 15. Google Maps visualization of the $99 \%$ conf uncertainty ellipse for a lightning strike near Complex 39A on 03 August 2009. Figure 15 shows a probability of $7.3 \%$ of the lightning strike occurring within the 0.45 nmi radius.

### 3.4 Test Set 4

The fourth type of testing analyzed six additional real-world lightning strikes in and around Space Launch Complexes 39A and 39B. These examples were generated based on an Electromagnetic Environmental Effects (EEE) panel request to run several case studies where there was camera verification of a lightning strike in the vicinity of Launch Complex 39A or 39B. The data used for this analysis are in Table 4. Both CGLSS and NLDN cases were examined, depending upon which sensor system recorded the stroke. Figures 16 through 21 show the probability results from these cases. As in section 3.3, all calculated probabilities were consistent with these additional real-world events.


Figure 16. Illustrates a probability of 92.1\% of a lightning strike of amplitude 38.9 kA detected by CGLSS occurring 0.32 nmi from the center of Launch Complex 39A on 8/16/2009.

| Figure | Semi- <br> major <br> axis <br> of <br> 50\% <br> CE <br> (nmi) | Semi- <br> minor <br> axis <br> of <br> 50\% <br> CE <br> (nmi) | Confidence | Heading (from true North) of semimajor axis | POI lat ( ${ }^{\circ} \mathrm{N}$ ) | POI Ion ( ${ }^{\circ} \mathrm{W}$ ) | Strike lat $\left({ }^{\circ} \mathrm{N}\right)$ | Strike Ion ( ${ }^{\circ} \mathrm{W}$ ) | Radius around POI (nmi) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | 0.15 | 0.05 | 0.99 | 300.8 | 28.60827 | 80.6041 | 28.6105 | 80.5987 | 0.45 |
| 17 | 0.3 | 0.2 | 0.99 | 82 | 28.60827 | 80.6041 | 28.6069 | 80.5087 | 0.45 |
| 18 | 0.2 | 0.2 | 0.99 | 95 | 28.60827 | 80.6041 | 28.6057 | 80.6085 | 0.45 |
| 19 | 0.2 | 0.1 | 0.99 | 49 | 28.60827 | 80.6041 | 28.6064 | 80.6050 | 0.45 |
| 20 | 0.1 | 0.05 | 0.99 | 70 | 28.62716 | 80.6208 | 28.6277 | 80.6207 | 0.45 |
| 21 | 0.1 | 0.05 | 0.99 | 72 | 28.62716 | 80.6208 | 28.6275 | 80.6202 | 0.45 |

Table 4. Input values used for scenarios shown in Figures 16 through 21. The abbreviations are the same as defined in Table 1.


Figure 17. Illustrates a probability of $72.1 \%$ of a lightning strike of amplitude -43.0 kA detected by NLDN occurring 0.26 nmi from the center of Launch Complex 39A on 8/16/2009.


Figure 18. Illustrates a probability of $77.7 \%$ of a lightning strike of amplitude -71.4 kA detected by NLDN occurring 0.28 nautical miles from the center of Launch Complex 39A on 10/14/2009.


Figure 19. Illustrates a probability of $97.2 \%$ of a lightning strike of amplitude 39.5 kA detected by CGLSS occurring 0.12 nmi from the center of Launch Complex 39A on 7/21/2008.


Figure 20. Illustrates a probability of $99.999975 \%$ of a lightning strike of amplitude -18.9 kA detected by CGLSS occurring 0.03 nmi from the center of Launch Complex 39B on 6/27/2009.


Figure 21. Illustrates a probability of $99.999925 \%$ of a lightning strike of amplitude -21.7 kA detected by CGLSS occurring 0.04 nmi from the center of Launch Complex 39B on 6/27/2009.

## 4 Summary

A technique has been developed to calculate the probability that any nearby lightning stroke is within any radius of any point of interest. In practice, this provides the probability that a nearby lightning stroke was within a key distance of a facility, rather than the error ellipses centered on the stroke. This process takes the bivariate Gaussian distribution of probability density provided by the current lightning location error ellipse for the most likely location of a lightning stroke and integrates it to get the probability that the stroke is inside any specified radius. This new facility-centric technique will be much more useful to the space launch customers and may supersede the lightning error ellipse approach discussed in [5], [6].

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## 6 References

1. Alfano, S., 2007: "Review of Conjunction Probability Methods for Short-term Encounters" AAS Paper No. 07-148, AAS/AIAA Space Flight Mechanics Meeting, Sedona, Arizona, 28 January-01 February 2007.
2. Alfano, S., 2009: "Satellite Collision Probability Enhancements" J. Guidance, Control, and Dynamics, 29(3), May-June 2009, pp. 588-592.
3. Chan, F. Kenneth, 2008. Spacecraft Collision Probability. The Aerospace Press, El Segundo, CA, 2008.
4. CRC Handbook of Tables for Probability and Statistics, 2nd edition, 1968: editor W. H. Beyer, Cleveland, OH: The Chemical Rubber Co., pp. 151-157.
5. Flinn, F. C., W. P. Roeder, M. D. Buchanan, and T. M. McNamara, 2010: Lightning Reporting at 45th Weather Squadron: Recent Improvements, 3rd International Lightning Meteorology Conference, 21-22 Apr 10.
6. Flinn, F. C., W. P. Roeder, D. F. Pinter, S. M. Holmquist, M. D. Buchanan, T. M. McNamara, M. McAleenan, K. A. Winters, P. S. Gemmer, M. E. Fitzpatrick, and R. D. Gonzalez, 2010: Recent Improvements in Lightning Reporting At 45th Weather Squadron, 14th Conference on Aviation, Range, and Aerospace Meteorology, 17-21 Jan 10, Paper 7.3, 14 pp.
7. Leleux, D., et. al., 2002: Probabilitybased Space Shuttle collision avoidance, Space Ops 2002 Conference, 20-24 Oct 2002, 18 pp.
8. Murphy, M. J., K. L. Cummins, N. W. S. Demetriades, and W. P. Roeder, 2008: Performance Of The New FourDimensional Lightning Surveillance System (4DLSS) At The Kennedy Space Center/Cape Canaveral Air Force Station Complex, 13th Conference on Aviation, Range, and Aerospace Meteorology, 20-24 Jan 07, 18 pp.
9. Roeder, W. P., 2010: The Four Dimension Lightning Surveillance System. 21st International Lightning Detection Conference, 21-22 Apr 10.
10. Roeder, W. P., J. W. Weems, and P. B. Wahner, 2005: Applications of the Cloud-To-Ground-Lightning-Surveillance-System Database. 1st Conference on Meteorological Applications of Lightning Data, 9-13 Jan 05, 5 pp.
